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(54) **NANOSTRUCTURED FRICTION ENHANCEMENT USING FABRICATED MICROSTRUCTURE**

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**B32B 7/12** (2006.01)

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(58) **Field of Classification Search** ..... **428/357, 428/364, 343**

See application file for complete search history.

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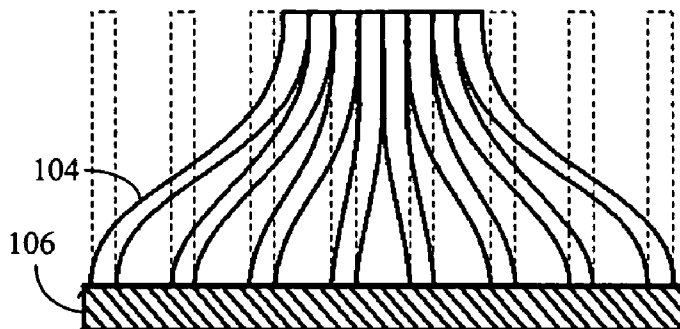
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(57) **ABSTRACT**

Described herein are fabricated microstructures to adhere in shear to a contact surface. A fabricated microstructure comprises a substrate and a plurality of nano-fibers attached to the substrate. The nano-fibers have an elasticity modulus E, an interfacial energy per unit length of contact w, a length L, a radius R, and are oriented at an angle  $\theta_o$  relative to the substrate. The length L of the nano-fibers is greater than  $0.627\theta_o R^2(E/w)^{1/2}$  with  $\theta_o$  in radians. Also described herein is a method of forming a fabricated microstructure to adhere in shear to a contact surface and a method of adhering in shear a fabricated microstructure to a contact surface.

**15 Claims, 4 Drawing Sheets**



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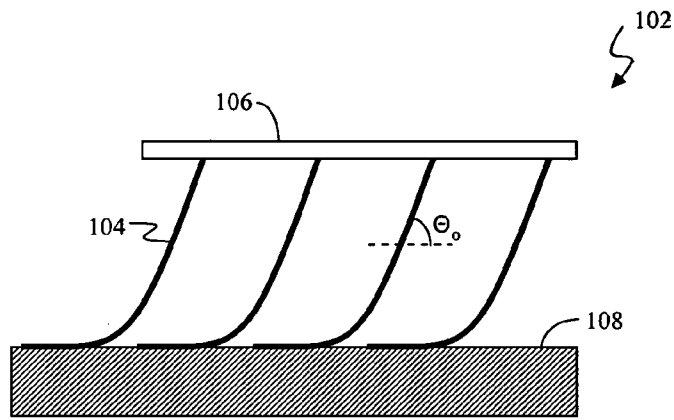


Fig. 1

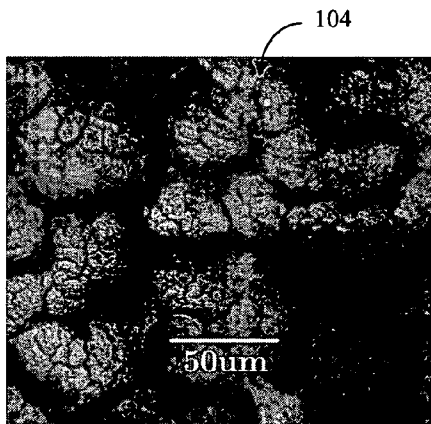


Fig. 2

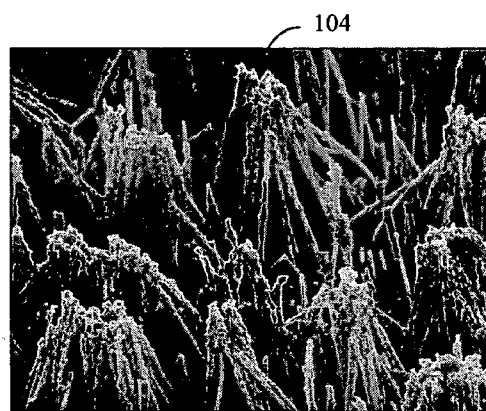


Fig. 3

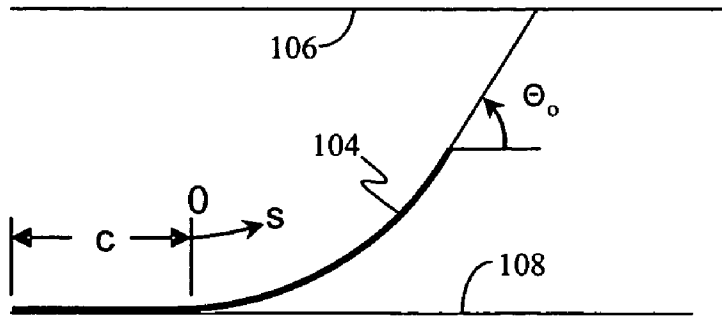


Fig. 4

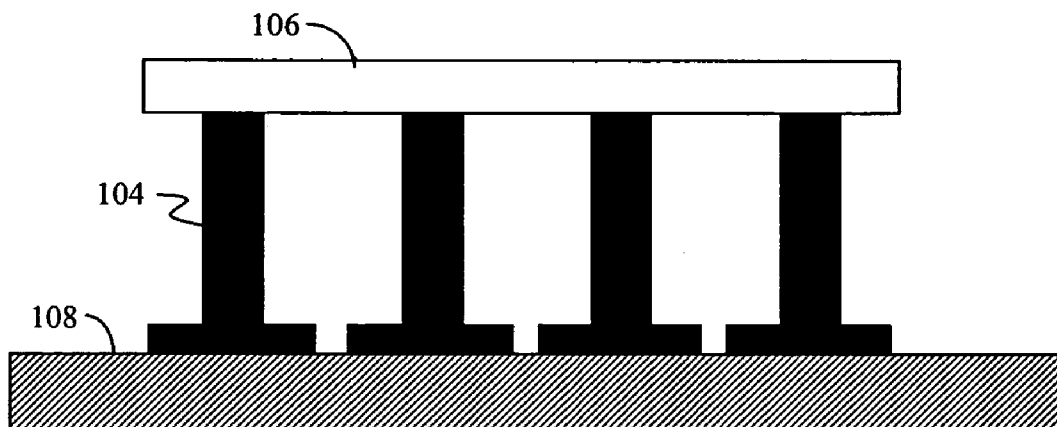


Fig. 5

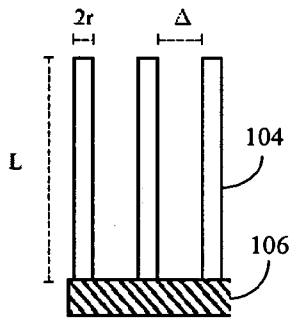


Fig. 6

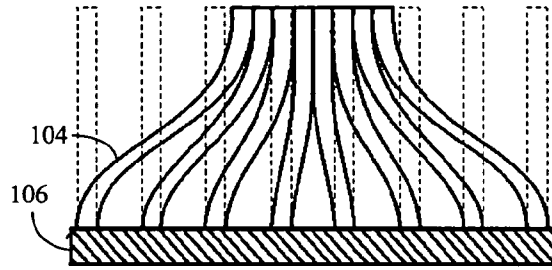


Fig. 7

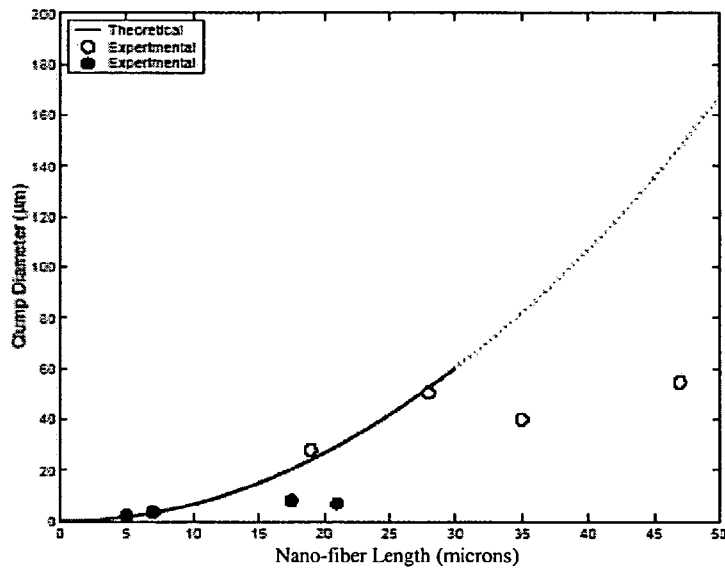


Fig. 8

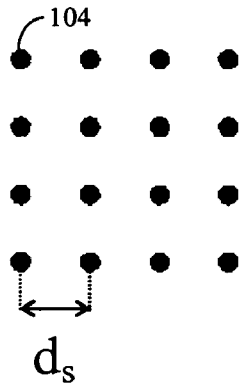


Fig. 9A

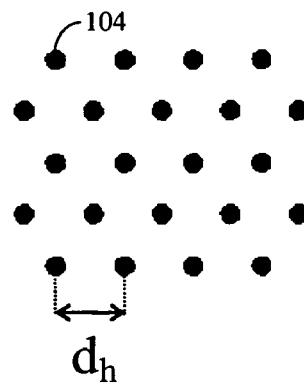


Fig. 9B

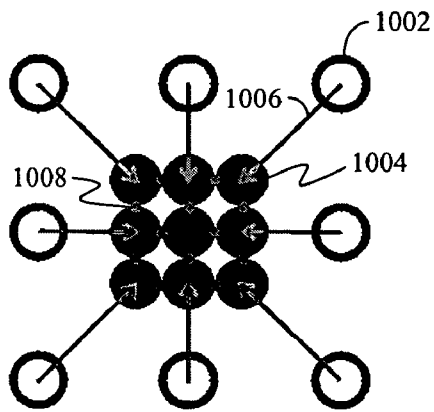


Fig. 10A

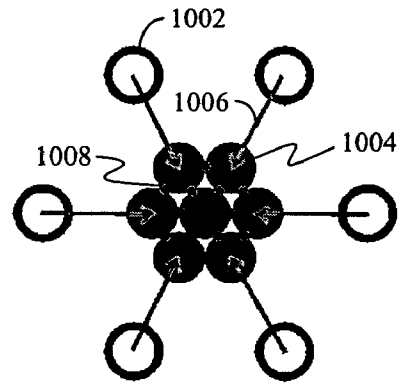


Fig. 10B

# NANOSTRUCTURED FRICTION ENHANCEMENT USING FABRICATED MICROSTRUCTURE

## CROSS-REFERENCE TO RELATED APPLICATIONS

This application claims the benefit under 35 USC 119(e) of U.S. Provisional Application No. 60/629,799, filed Nov. 19, 2004, which is incorporated in its entirety herein by reference.

## STATEMENT REGARDING FEDERALLY SPONSORED RESEARCH OR DEVELOPMENT

This invention was made with Government support under Grant (contract) No. NMA 501-03-1-2017 awarded by the National Imagery and Mapping Agency and No. EEC-0304 730 awarded by the National Science Foundation. The Government has certain rights in this invention.

## BACKGROUND

### 1. Field

This application generally relates to the fabrication and utilization of micron-scale structures. More particularly, this application relates to nanostructured friction enhancement using a fabricated nanostructure.

### 2. Related Art

There is an ongoing need for improved adhesives. Improved adhesives have applications ranging from everyday aspects of life (e.g., tape, fasteners, and toys) to high technology (e.g., removal of microscopic particles from semiconductor wafers, transporting fiber optic devices, and assembly of sub-mm mechanisms, particularly those including micro-fabricated components, or components that cannot tolerate grippers, adhesives, or vacuum manipulators).

Adhesive mechanisms in nature have been studied, but have not been fully understood or exploited. For example, Geckos are exceptional in their ability to rapidly climb up smooth vertical surfaces. The mechanism of adhesion used by Geckos, Anolis lizards, some skinks, and some insects, has been debated for nearly a century.

## SUMMARY

Biological nanohair adhesive systems, found, for example, in geckos, feature setae (hairs) with a hierarchical branching structure terminating in small, flat plates, called spatulae. Gecko setae observed in nature are not found in a clumped state, i.e., stuck to one another. Adhesive nano-fibers inspired by these biological examples have traditionally been designed to avoid clumping of the hairs. Previous work provides necessary conditions on hair geometry to avoid clumping, for example 1) under the assumption that a spatula at the end of the hair is capable of providing up to some fixed maximum force (see, Metin Sitti and Ronald S. Fearing, Synthetic Gecko Foot-Hair Micro/Nano-Structures for Future Wall-Climbing Robots, IEEE International Conference on Robotics and Automation, September 2002, which is incorporated herein by reference in its entirety) or 2) under the assumption that hairs stick along their length due to surface forces (see, A. Jagota and S. Bennison, Mechanics and Adhesion through a Fibrillar Microstructure, Integrative and Comparative Biology, 42:1140-1145, 2002, which is incorporated herein by reference in its entirety). Engineered nano-fiber systems (see, A. K. Geim, et al. Microfabricating adhe-

sive mimicking gecko foot-hair, Nature Materials 2, pp 461-463, Jun. 1, 2003, which is incorporated herein by reference in its entirety) have expressly avoided configurations in which hairs clump, choosing instead to employ short, fat hairs. In Geim, for example, the hairs are 0.5  $\mu\text{m}$  in diameter, 2  $\mu\text{m}$  long with centers spaced 1.6  $\mu\text{m}$  apart.

Described herein are fabricated microstructures to adhere in shear to a contact surface. A fabricated microstructure comprises a substrate and a plurality of nano-fibers attached to the substrate. The nano-fibers have an elasticity modulus E, an interfacial energy per unit length of contact w, a length L, a radius R, and are oriented at an angle  $\theta_o$  relative to the substrate. The length L of the nano-fibers is greater than  $0.627\theta_o R^2(E/w)^{1/2}$  with  $\theta_o$  in radians.

Also described herein is a method of forming a fabricated microstructure to adhere in shear to a contact surface. The method comprises forming a substrate and forming a plurality of nano-fibers attached to the substrate. The nano-fibers can have an elasticity modulus E, an interfacial energy per unit length of contact w, a length L, a radius R, and can be oriented at an angle  $\theta_o$  relative to the substrate. The length L of the nano-fibers can be greater than  $0.627\theta_o R^2(E/w)^{1/2}$  with  $\theta_o$  in radians.

Also described herein is a method of adhering in shear a fabricated microstructure to a contact surface. The method comprises obtaining a substrate having a plurality of nano-fibers attached to the substrate and placing the substrate on the contact surface. The nano-fibers can have an elasticity modulus E, an interfacial energy per unit length of contact w, a length L, a radius R, and can be oriented at an angle  $\theta_o$  relative to the substrate. The length L of the nano-fibers can be greater than  $0.627\theta_o R^2(E/w)^{1/2}$  with  $\theta_o$  in radians.

## DESCRIPTION OF DRAWING FIGURES

FIG. 1 illustrates a fabricated microstructure array to adhere in shear to a contact surface.

FIG. 2 illustrates clumps of epoxy nano-fibers approximately arranged in a hex-lattice configuration.

FIG. 3 illustrates clumps of polyimide nano-fibers arranged in an irregular-lattice configuration.

FIG. 4 illustrates that when a nano-fiber adheres in shear to a contact surface, a portion of the length of the nano-fiber makes contact with the contact surface.

FIG. 5 illustrates an embodiment of the fabricated microstructure where the tip geometry of the nano-fiber is a T-shaped terminal.

FIG. 6 illustrates nano-fibers disposed on a substrate at a certain distance from each another.

FIG. 7 illustrates a clump of nano-fibers.

FIG. 8 illustrates theoretical and experimentally observed clump diameter as a function of nano-fiber length.

FIG. 9A illustrates a square lattice configuration.

FIG. 9B illustrates a hexagonal lattice configuration.

FIG. 10A illustrates the energies involved with joining a small clump in a square lattice configuration.

FIG. 10B illustrates the energies involved with joining a small clump in a hexagonal lattice configuration.

## DETAILED DESCRIPTION

With reference to FIG. 1, in one exemplary embodiment, a fabricated microstructure array **102** to adhere in shear to a contact surface **108** is depicted. In the present exemplary embodiment, array **102** includes a plurality of nano-fibers **104** attached to a substrate **106**. In the present exemplary embodiment, nano-fibers **104** have an elasticity modulus E, an inter-

facial energy per unit length of contact  $w$ , a length  $L$ , and a radius  $R$ . To improve adhesion to contact surface **108**, nano-fibers **104** are biased at an angle  $\theta_o$  relative to substrate **106** (see, U.S. patent application Ser. No. 10/197,763, titled ADHESIVE MICROSTRUCTURE AND METHOD OF FORMING SAME, filed on Jul. 17, 2002, which is incorporated herein by reference in its entirety).

In the present exemplary embodiment, nano-fibers **104** have a high aspect ratio (ratio of length  $L$  to radius  $R$ ). In particular, length  $L$  of nano-fibers **104** is greater than  $0.627\theta_o R^2(E/w)^{1/2}$  with  $\theta_o$  in radians. The high aspect ratio of nano-fibers **104** allows the ends of nano-fibers **104** to bend to come in intimate contact with contact surface **108** without storing enough elastic strain energy to cause the ends to spring off contact surface **108**. To prevent spring back even further, the ends of nano-fibers **104** can be pre-bent, for example by plastic deformation. In this manner, the ends of nano-fibers **104** with a high aspect ratio act as spatulas without requiring specially formed spatular structures. In one exemplary embodiment, nano-fibers **104** can provide adhesion with a ratio between shear force and normal force of 300 to 1.

In the present exemplary embodiment, nano-fibers **104** are disposed on substrate **106** with a high packing density. In particular, nano-fibers **104** are disposed on substrate **106** with a linear spacing greater than  $0.188(L/R)^2(w/E)^{1/2}$ . Alternatively, the linear spacing can be greater than  $0.445(L/W)^2(w/E)^{1/2}$ , which allows formation of small clumps. Due to surface forces (van der Waals or capillary action), an individual nano-fiber **104** with a high aspect ratio, though able to support its own weight, may easily become attached to substrate **106**. The high packing density allows nano-fibers **104** to form clumps, which allows individual nano-fibers **104** to mutually support each other. Preload forces can supply enough energy to break apart the clumps and allow nano-fibers **104** to come into contact with contact surface **108** to which array **102** is being applied. It should be recognized that there are design tradeoffs in the aspect ratio of nano-fibers **104** (higher ratios allow nano-fibers **104** to conform to surfaces better, but form bigger clumps) and clump size (bigger clumps keep more nano-fibers **104** supported, but require more energy to break apart to achieve contact with contact surface **108**).

In the present exemplary embodiment, nano-fibers **104** are disposed on substrate **106** in a square-lattice configuration. As will be described in more detail below, disposing nano-fibers **104** on substrate **106** using a square-lattice configuration allows interaction between clumps of nano-fibers **104** and contact surface **108** to more easily break up the clumps and allow nano-fibers **104** to adhere to contact surface **108**.

For example, with reference to FIG. 2, clumps of epoxy nano-fibers **104** are depicted that are 0.2 microns in diameter, 60 microns in length, with centers spaced 0.3 microns apart in an approximately hex-lattice configuration. With reference to FIG. 3, clumps of polyimide nano-fibers **104** are depicted that are 0.6 microns in diameter, 20  $\mu\text{m}$  in length, with centers approximately 1.8 microns in an irregular-lattice configuration.

#### I. Adhesion Force of Nano-Fibers

With reference to FIG. 4, when a nano-fiber **104** adheres in shear to contact surface **108**, a portion of the length of nano-fiber **104** makes contact with contact surface **108**. As demonstrated in the following analysis, nano-fiber **104** must be sufficiently slender (high aspect ratio) in order for such a configuration to be mechanically stable under external loading. In addition, nano-fiber **104** can be fabricated with a curve

at the end to reduce elastic bending energy required to make side contact with substrate **106**, and increase stability.

#### A. Peel Strength

As depicted in FIG. 4, when nano-fiber **104** adheres in shear to contact surface **108**, nano-fiber **104** is oriented an angle  $\theta_o$  with respect to contact surface **108**, and makes contact with contact surface **108** over a length  $L-a$ , such that  $a$  is the length of the unattached portion of nano-fiber **104**. For a normal pull-off load  $P$  acting at the base of nano-fibers **104**, the total potential energy of the system is:

$$U_t = wa + \int_0^a \frac{EI}{2} (\theta')^2 ds - \int_0^a P \sin(\theta) ds \quad (1)$$

where,  $\theta(s)$  is the slope of nano-fiber **104** at a distance  $s$  from contact,  $E$  is the elastic modulus,  $I$  is the area moment of inertia, and  $w$  is the interfacial energy per unit length of contact.

At equilibrium, the total potential is minimum with respect to the configuration variable  $a$  and the function  $\theta(s)$ . Assuming that  $\theta_o$  is sufficiently small such that  $\sin \theta \approx \theta$ , equation (1) simplifies to:

$$U_t \approx wa + \int_0^a \left[ \frac{EI}{2} (\theta')^2 - P\theta \right] ds. \quad (2)$$

The integral is minimized with respect to  $\theta(s)$  if the integrand, defined as  $F(s, \theta, \theta')$ , satisfies the equation:

$$\frac{\partial F}{\partial \theta} - \frac{d}{ds} \frac{\partial F}{\partial \theta'} = 0. \quad (3)$$

for the boundary conditions  $\theta(0)=0$  and  $\theta(a)=\theta_o$ . (See, Lanczos, C, The Variational Principles of Mechanics, New York: Dover, pg. 60 (1970), which is incorporated herein by reference in its entirety.) Solving the resulting ODE for  $\theta(s)$  and substituting this into equation (2) gives an expression for  $U_t$  only in terms of the length  $a$ . Lastly, setting  $\partial U_t / \partial a = 0$ , it follows that at equilibrium:

$$P = \frac{2}{a^2} (a\sqrt{2EIw} - EI\theta_o), \quad (4)$$

which is largest when  $a = \theta_o \sqrt{2EI/w}$ . Hence, the maximum allowable pull-off force (i.e., peel strength) is:

$$T = \begin{cases} w/\theta_o & \text{if } L \geq \theta_o \sqrt{2EI/w} \\ \frac{2}{L^2} (L\sqrt{2EIw} - EI\theta_o) & \text{otherwise} \end{cases} \quad (5)$$

#### B. Shear Strength

If only a shear force,  $V$ , is applied, then bond failure is more likely to depend on strain energy stored in elongation of nano-fiber **104** rather than bending. If, under the presence of a constant  $V$ , the length of the unattached portion of nano-



fiber **104** increases by an infinitesimally small amount  $\delta a$ , the potential energy changes by an amount:

$$\delta U_t = w\delta a + \frac{1}{2E} \left(\frac{V}{A}\right)^2 A\delta a - V \left(\frac{V}{EA}\right) \delta a \quad (6)$$

where the first term represents the increase in free surface energy, the second term is the increase in elastic strain energy, and the final term follows from the work of the external shear load.

Since  $U_t$  is minimized at equilibrium,  $\delta U_t = 0$ , which implies that:

$$V = \sqrt{2EAw} \quad (7)$$

Approximating  $T \approx (2/L)\sqrt{2EIw}$  and noting that  $I = \pi R^4/4$  and  $A = \pi R^2$ , where  $R$  is the radius of nano-fiber **104**, the ratio between the shear and peel strength is found to be equal to the aspect ratio  $L/R:1$ . This is a very large difference and for more slender nano-fibers **104** the ratio can be as high as 300:1. It should be noted that for tip geometries in which peeling is not permitted, such as a sphere or a T-shaped terminal (as depicted in FIG. 5), the shear to pull off ratio is greatly reduced to 0.1:1 or 1:1, depending on the magnitude of the friction coefficient.

### C. Enhanced Friction

With reference to FIG. 1, assuming that stresses are uniformly distributed among nano-fibers **104**, the shear resistance is  $n\sqrt{2EAw}$ , where  $n$  is the number of nano-fibers **104** in contact with contact surface **108**. This assumes that nano-fibers **104** are being dragged parallel to their axis of contact. If nano-fibers **104** are pulled in a direction that is deflected from the contact axis by an angle  $\alpha$ , then the necessary shear for peeling is better approximated by  $\min\{\sqrt{2EAw}, w/(1 - \cos \alpha)\}$ .

According to equation (1), the stiffness,  $EI/L^2$ , of an individual nano-fiber **104** is less than  $2w/\theta_o^2$  in order for it to be able to make contact along its side during pull-off. The critical buckling strength, however, is  $\pi^2 EI/4L^2$ , which implies that for compressive loads greater than  $\pi^2 w/2\theta_o^2$ , contact surface **108** will make direct contact with substrate **106**. Noting that  $w$  is typically  $\sim 1$  nN, under most finite compressive loads, sliding involves only contact surface **108** and substrate **106**, in which case the frictional resistance is approximately  $\mu P$ , where  $\mu$  is the coefficient of friction and  $P$  is the compressive load. Typically,  $\mu$  is between 0.1 and 1.

Combining the two cases of zero and finite compressive load, array **102** follows Coulomb's law of friction:

$$V = \mu P + V_{ad} \quad (8)$$

where  $\mu$  is between 0.1 and 1 and the shear strength  $V_{ad}$  is the sum of

$$\min\{\sqrt{2EAw}, w/(1 - \cos \alpha)\}$$

all nano-fibers **104** on array **102** in contact with contact surface **108**. As  $P$  approaches zero, the value of  $V/P$  approaches infinity since  $V_{ad}$  is finite.

### II. Clump Size Prediction

With reference to FIG. 6, nano-fibers **104** having length  $L$  and radius  $R$  are disposed on substrate **106**, and are separated by a distance  $\Delta$  from each other. Nano-fibers **104** can bind to each other rather than to contact surface **108**. The distance  $\Delta$  that adjacent nano-fibers **104** must be separated in order to avoid binding can be expressed in terms of the design parameters  $E$ ,  $I$ ,  $w$ , and  $L$ :

$$\Delta > \frac{L^2}{6} \sqrt{\frac{w}{EI}} = \frac{1}{3\sqrt{\pi}} \left(\frac{L}{R}\right)^2 \sqrt{\frac{w}{E}} \approx 0.188 \left(\frac{L}{R}\right)^2 \sqrt{\frac{w}{E}} \quad (9)$$

With reference again to FIG. 1, in the absence of any external load, it follows from equation (1), with  $P=0$ , that side contact with contact surface **108** is only possible if:

$$L > \theta_o \sqrt{\frac{EI}{2w}} = \frac{\sqrt{\pi}}{2\sqrt{2}} \theta_o R^2 \sqrt{\frac{E}{w}} \approx 0.627 \theta_o R^2 \sqrt{\frac{E}{w}} \quad (10)$$

This implies, then, that for a fixed stiffness,  $EI$ , nano-fibers **104** must be spaced at least a distance  $(\theta_o^2/12)\sqrt{EI/w}$  apart. For  $I = \pi R^4/4$ , where  $R$  is the radius of nano-fibers **104**, and assuming typical values of  $E=1$  GPa and  $w=1$  nN, the necessary spacing of nano-fibers **104** is on the order of  $R^2/(0.01 \text{ um})$ . Hence, a suitable packing density can be achieved with nano-fibers **104** of radius 100 nm, whereas larger nano-fibers **104** with micron width would need to be exceedingly long for side contact with contact surface **108**, and hence excessively sparse to avoid inter-fiber binding.

Treating a clump of nano-fibers **104** as a single large nano-fiber **104**, it follows from linear beam theory that the strain energy for a clump of  $n$  nano-fibers **104** under a shear load  $V$  is  $U_{el,1} = V^2 L^3 / 6n^2 EI$ . If the outer ring of nano-fibers **104**, which number  $m = \pi\sqrt{n}$ , detach from the clump, then the clump radius reduces to  $(\sqrt{n}-2)R$ , resulting in an area fraction of  $A_c = (\sqrt{n}-2)^2/n$  for the entire array. The elastic energy, becomes:

$$U_{el,2} = (VA_c)^2 \frac{L^3}{6EI} \frac{1}{(\sqrt{n}-2)^4} + m[V(1-A_c)]^2 \frac{L^3}{6EI} \quad (11)$$

where the first term is the elastic energy of the clump and the second term is the sum of the elastic energy in the detached nano-fibers **104**. Note that it is assumed here that the shear load  $V$  is uniformly distributed among the nano-fibers **104**. Defining  $W_{ad}$  to be the net change in surface energy for each of the circumferential nano-fibers **104** that binds to contact surface **108** after detaching from the clump, the change in total energy is approximately  $\Delta U = U_{el,2} - U_{el,1} - mW_{ad}$ . By the principle of least work,  $\Delta U = 0$  at equilibrium. Solving for  $V$ :

$$V = \frac{1}{2} \frac{n}{(\sqrt{n}-1)} \sqrt{\frac{3EIW_{ad}}{2L^3}} \approx \frac{1}{2} \sqrt{\frac{3EIW_{ad}}{n-2L^3}} \quad (12)$$

This is the force needed to begin breaking the clump of nano-fibers **104**. The necessary force increases with clump size, and so it is desirable for the clumps to be as small as possible.

In the case that clumping does occur, the amount of nano-fibers **104** in each clump can be predicted for a specific geometry and spacing of nano-fibers **104**. Assuming that nano-fibers **104** clump in the manner illustrated in FIG. 7:

$$w_p \approx 0.89 \frac{L^2}{R\Delta} \sqrt{\frac{w}{E}} \quad (13)$$

where  $w_p$  is the width of the clump and  $\gamma$  is the surface energy of the material. This model tends to overestimate observed clump size, as shown in FIG. 8, but serves as a useful tool for nano-fiber **104** design.

### III. Lattice Structures

Planar regular lattices can either be square (FIG. 9A) or hexagonal (FIG. 9B). With reference to FIG. 9A, in a square lattice, if the inter-fiber spacing is  $d_s$ , then the density (nano-fibers **104** per unit area) will be:

$$\rho = \frac{1}{d_s^2}. \quad (14)$$

With reference to FIG. 9B, in a hexagonal lattice with inter-fiber spacing  $d_h$ , then the density will be:

$$\rho = \frac{2\sqrt{3}}{3d_h^2}. \quad (15)$$

It follows that for equivalent densities, square packing will have smaller inter-fiber spacing than hexagonal packing. Specifically, choosing inter-fiber spacing of:

$$d_h = \sqrt{\frac{2\sqrt{3}}{3}} d_s \approx 1.075d_s \quad (16)$$

provides equivalent densities for hexagonal and square lattices. Since adhesion forces are monotonic in the number of engaged nano-fibers **104**, hexagonal packing would naively seem beneficial, since for a given inter-fiber spacing, more nano-fibers **104** can be packed into an area. Some analysis, however, demonstrates that square packing offers advantages over hexagonal packing with respect to the energy clumping.

In particular, with reference to FIGS. 9A and 9B, when a neighboring nano-fiber **104** joins the clump, the strain energy in that nano-fiber **104** increases. This strain energy is monotonic in distance, and is written as  $E_{st}(d)$ , where  $d$  is the distance the tip must move. For the present, consider

$$E_{st}(d) = \frac{1}{2}kd^2,$$

though the argument holds for a more general class of strain energies (for example, if the strain energy is monotonic increasing and convex in  $d$ ). For the square lattice (FIG. 9A), the total strain energy stored in the eight neighbors is:

$$\begin{aligned} E_{st,s} &= 4E_{st}(d_s) + 4E_{st}(\sqrt{2}d_s) \\ &= 6kd_s^2 \end{aligned} \quad (17)$$

while for the hexagonal lattice (FIG. 9B) the strain energy stored in the six neighbors is:

$$\begin{aligned} E_{st,h} &= 6E_{st}(d_h) \\ &= 2\sqrt{3}kd_s^2 \end{aligned} \quad (18)$$

In this region for both hexagonal and square packing, the number of contacts with other nano-fibers **104** in this small clump is **12**. For now, assume that each of these contacts provides the same reduction in adhesive potential energy,  $-E_{ad}$ . (Actually, in the clumping model described herein, nano-fibers **104** that are farther away would have provided a smaller drop in adhesive potential energy, which would further benefit the square lattice configuration.) Thus, the total change in potential for square packing is:

$$\begin{aligned} E_s &= 4E_{st}(d_s) + 4E_{st}(\sqrt{2}d_s) - 12E_{ad} \\ &= 6kd_s^2 - 12E_{ad} \end{aligned} \quad (19)$$

and for hexagonal packing is:

$$\begin{aligned} E_h &= 6E_{st}(d_h) - 12E_{ad} \\ &= 2\sqrt{3}kd_s^2 - 12E_{ad} \end{aligned} \quad (20)$$

With the current form of  $E_{st}(d)$  (or more generally, if  $E_{st}(d)$  is convex and monotonically non-decreasing in  $d$ , a quite natural assumption for an elastic beam, point forces at the end of the beam give a quadratic strain energy), then the potential energy of the clumped square packed system will be higher than the potential energy of the clumped hexagonal packed system:

$$\begin{aligned} E_s - E_h &= 4E_{st}(d_s) + 4E_{st}(\sqrt{2}d_s) - 6E_{st}(d_h) \\ &= (6 - 2\sqrt{3})kd_s^2 > 0, \end{aligned} \quad (21)$$

Thus, the square packed system is more difficult to get into and easier to get out of the clumped configuration. For densely packed nano-fibers **104**, nano-fibers **104** are normally in the clumped state. With reference to FIG. 1, square packing will make it easier for interaction with contact surface **108** to break up the clumps and allow nano-fibers **104** to adhere to contact surface **108**.

FIG. 10A depicts the energies involved with joining a small clump in a square-lattice configuration. FIG. 10B depicts the energies involved with joining a small clump in a hexagonal-lattice configuration. In FIGS. 10A and 10B, locations **1002** correspond to the location of the base of nano-fibers. Locations **1004** correspond to the location of the tips of nano-fibers. Arrows **1006** indicate the distance to join the clump. Dots **1008** indicate contacts made with other nano-fibers.

### IV. Interfacial Energy

The interfacial energy per unit length between a pair of contacting nano-fibers, herein referred to as  $w$ , can be reasonably estimated by analogy to JKR contact for spheres. (See K. L. Johnson, K. Kendall, A. D. Roberts, Surface Energy and the Contact of Elastic Solids, Proc. Roy. Soc. Lond. A, Vol.

324, pp. 301-313 (1971), which is incorporated herein by reference in its entirety.) Similarly, two parallel cylinders of radius R, Young's modulus E, and Poisson modulus  $\nu$ , will make contact over a finite area even in the absence of an external load as long as a sufficient preload is applied and surface energy,  $\gamma$ , is assumed. The total energy, i.e., the sum of strain and surface energy, per unit length for two cylinders contacting with width  $2c$  along their length, is given by:

$$U = \frac{\pi E}{64(1-\nu^2)R^2} c^4 - 4\gamma c \tag{22}$$

Solving

$$\frac{\partial U}{\partial c} = 0$$

for  $c^*$  and solving for the interfacial energy  $w$  gives:

$$w = -U(c^*) = 12 \left( \frac{(1-\nu^2)R^2\gamma^4}{\pi E} \right)^{\frac{1}{3}} \tag{23}$$

V. Predicted Forces for Adhesive Arrays

With reference to FIG. 1, the center-to-center spacing for nano-fibers **104** is  $\Delta + 2R$ . From this, the density of nano-fibers **104** in a square packed array is:

$$\rho = \frac{1}{(\Delta + 2R)^2} \tag{24}$$

The density in a hexagonally packed array can be found in a similar fashion. An upper bound on the predicted pulloff forces is given by assuming all nano-fibers **104** in array **102** engage with contact surface **108**. This is a loose upper bound, since a small percentage of nano-fibers **104** generally engage. The bound on normal pulloff force for array **102** is given by  $\rho T$ , where T is given by Equation 5, while the bound on shear pulloff force is  $\rho V$ , where V is given by equation 7. Specifically, the shear pulloff force of array **102** is:

$$V_{array} = \sqrt{2\pi} \frac{\sqrt{ER^2w}}{(\Delta + 2R)} \tag{25}$$

The ratio of shear to normal remains the same as for the individual hair.

We claim:

1. A fabricated microstructure to adhere in shear to a contact surface, the fabricated microstructure comprising: a substrate; and a plurality of nano-fibers attached to the substrate, wherein the plurality of nano-fibers pack together into one or more clumps of mutually-supporting nano-fibers when not in contact with the contact surface, wherein the clumps break apart when the nano-fibers in the clumps come into contact with the contact surface; wherein the nano-fibers have an elasticity modulus E, an interfacial energy per unit length of contact w, a length

L, a radius R, and are biased at an angle  $\theta_o$  relative to the substrate when the nano-fibers are not clumped together, wherein the length L of the nano-fibers is greater than  $0.627\theta_o R^2(E/w)^{1/2}$  with  $\theta_o$  in radians,

- and wherein each nano-fiber includes a first end attached to the substrate and a free second end opposite the first end, and wherein a portion of the length of the nano-fibers contact the contact surface.
2. The fabricated microstructure of claim 1, wherein the nano-fibers are disposed on the substrate with a linear spacing greater than  $0.188(L/R)^2(w/E)^{1/2}$ .
3. The fabricated microstructure of claim 2, wherein the angle  $\theta_o$  is between 0.35 and 1.22 radians, radius R is between  $0.025 \mu\text{m}$  and  $1 \mu\text{m}$ .
4. The fabricated microstructure of claim 3, wherein the length L of the nano-fiber is greater than 5 microns.
5. The fabricated microstructure of claim 1, wherein the plurality of nano-fibers is disposed on the substrate in a square-lattice configuration.
6. The fabricated microstructure of claim 1, wherein a ratio of the length L to the radius R is equal to a ratio of shear force to normal pull-off force.
7. The fabricated microstructure of claim 6, wherein the ratio of the length L to the radius R is greater than 20 to 1.
8. The fabricated microstructure of claim 1, wherein, when the nano-fibers adhere in shear to the contact surface, the nano-fibers bend and adhere along the portion of their length.
9. The fabricated microstructure of claim 1, wherein the nano-fibers are cylindrical.
10. The fabricated microstructure of claim 1, wherein  $\theta_o$  is between 0.35 and 1.22 radians, and wherein the nano-fibers are disposed on the substrate with a linear spacing greater than  $0.188(L/R)^2(w/E)^{1/2}$ .
11. The fabricated microstructure of claim 1, wherein radius R is between  $0.1 \mu\text{m}$  and  $0.3 \mu\text{m}$ .
12. A fabricated microstructure to adhere in shear to a contact surface, the fabricated microstructure comprising: a substrate; and a plurality of nano-fibers attached to the substrate, wherein the plurality of nano-fibers pack together into one or more clumps of mutually-supporting nano-fibers when not in contact with the contact surface, wherein the clumps break apart when the nano-fibers in the clumps come into contact with the contact surface, wherein the nano-fibers have an elasticity modulus E, an interfacial energy per unit length of contact w, a length L, a radius R, and are biased at an angle  $\theta_o$  relative to the substrate when the nano-fibers are not clumped together, wherein  $\theta_o$  is between 0.35 and 1.22 radians, wherein the length L of the nano-fibers is greater than  $0.627\theta_o R^2(E/w)^{1/2}$  with  $\theta_o$  in radians, wherein each nano-fiber includes a first end attached to the substrate and a free second end opposite the first end, and wherein a portion of the length of the nano-fibers contact the contact surface.
13. The fabricated microstructure of claim 12, wherein the nano-fibers are disposed on the substrate with a linear spacing greater than  $0.188(L/R)^2(w/E)^{1/2}$ .
14. The fabricated microstructure of claim 13, wherein, radius R is between  $0.025 \mu\text{m}$  and  $1 \mu\text{m}$ , and wherein the length L of the nano-fiber is greater than 5 microns.
15. The fabricated microstructure of claim 12, wherein the plurality of nano-fibers are disposed on the substrate in a square-lattice configuration.